



**STRATUM**  
RESERVOIR

# RELATIVE PERMEABILITY BEST PRACTICE FOR STEADY STATE METHOD

Helene Berntsen Auflem

[Helene.Auflem@stratumreservoir.com](mailto:Helene.Auflem@stratumreservoir.com)

Chief Engineer SCAL (Trondheim, Norway)



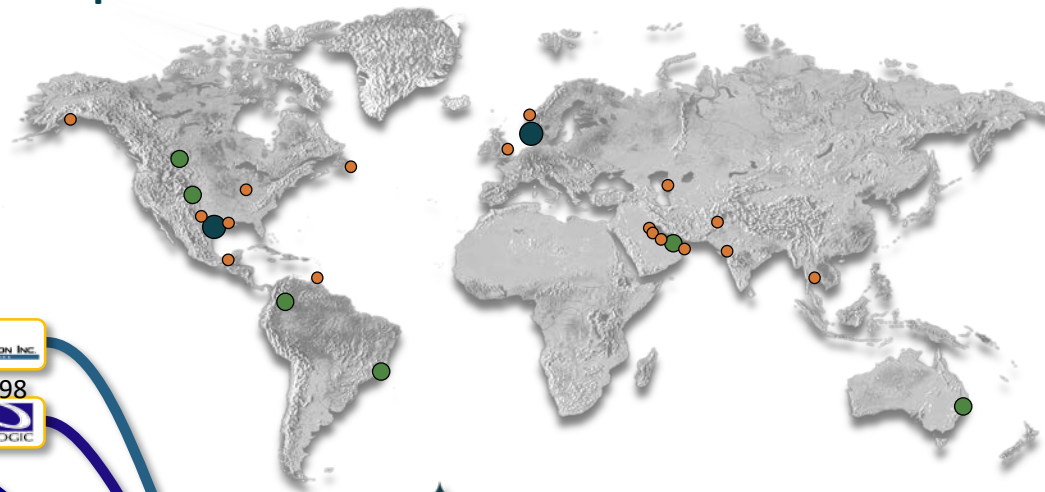
**Qatar Chapter**

# OUTLINE

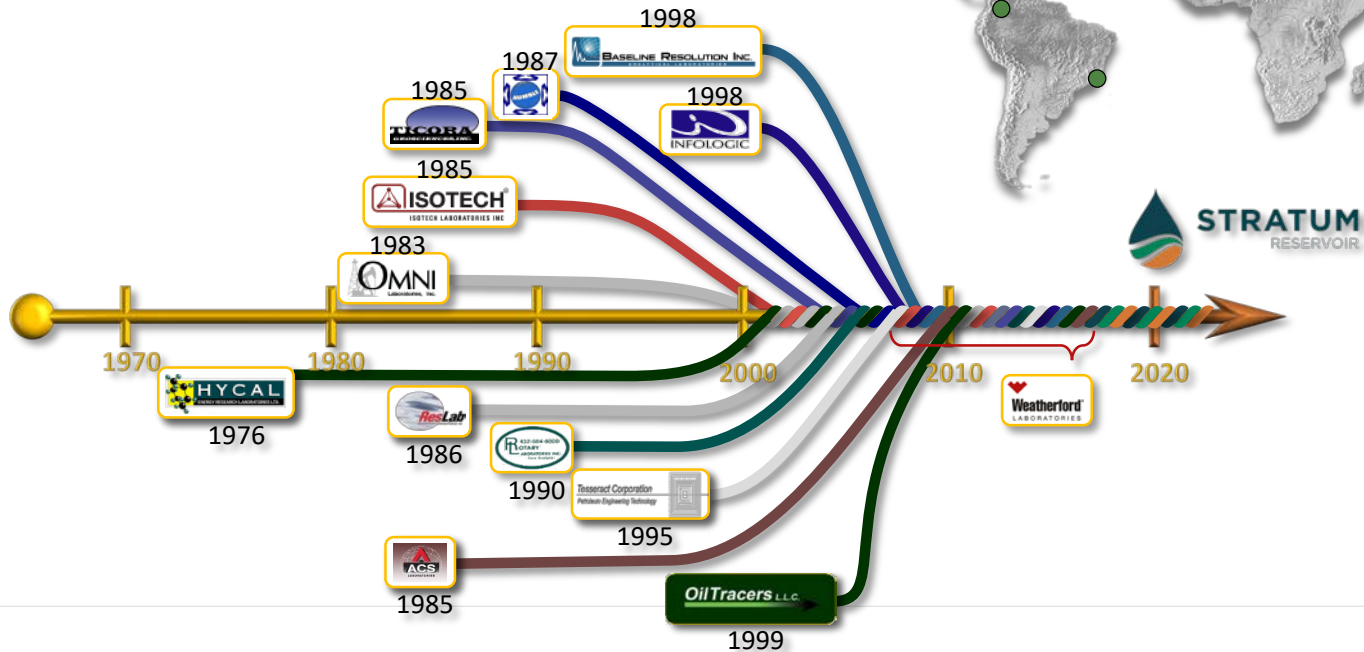
1. Stratum Reservoir introduction
2. Short introduction to Relative Permeability
3. Relative Permeability by Steady State method

# STRATUM RESERVOIR - History and Expertise

23 Labs/ 16 Countries



Decades of experience, new applications.



# Key Aspects

## Global Experience and Best Practices

Stratum Reservoir has gained extensive experience in both Conventional and Unconventional reservoirs worldwide.

## Subject Matter Experts (SME's)

SME's are made freely available, covering each discipline. Our specialists are able to assist with each stage of the program –from inception and design to integration and interpretation of all datasets.

## Program Design and Objectives

Stratum Reservoir maintains a dynamic technical and managerial approach to ensure any program remains optimized against project objectives and deliverables.



# Detailed Laboratory Services Overview



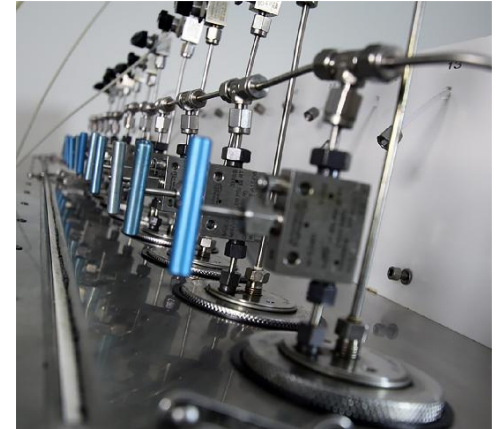
## SERVICES & CAPABILITIES

- Global Wellsite Core Preservation & Stabilization
- DECT Scanning (Mineral Modeling)
- Routine Core Analysis
- **Special Core Analysis**
- Rock Mechanics
- Unconventional Core Analysis
- Petrographic Analysis
- Formation Damage Evaluation
- Geochemistry / Production Allocation
- Express Lab cuttings analysis
- PVT / Fluid Phase Behavior
- PVT for Unconventional
- Oilfield Water Analysis
- **IOR/ EOR**
- Pressurized Rotary Sidewall Core Analysis
- H<sub>2</sub>S Identification and Mitigation
- Core to Log Integration
- Basin Data Studies
- Core Storage Expertise



# SCAL - Petrophysics

- Rock Characterization Studies (XRD, SEM, THS)
- Electrical properties studies at reservoir pressure and temperature (FF, Kw, m-exp.)
- Porosity and Permeability as a function of Reservoir Pressure
- Pc-RI Capillary Pressure and Resistivity Studies Drainage and Imbibition (RI, n-exp., Swi, Sor)
- Capillary Pressure by Mercury Injection Analysis (MICP)
- Semi-Dynamic Electrical Properties Analysis (CI)
- Clay Conductivity Studies (Co/Cw, CEC)
- Nuclear Magnetic Resonance
- Capillary Threshold Pressure Analysis and Seal Capacity Studies (PcTh)
- Water Sensitivity and Critical Velocity Tests (Fines Migration)





# SCAL – Dynamics and Advanced Testing

## SCAL Semi Reservoir Conditions:

- Capillary pressure by centrifugation
- Relative Permeability by flooding with In Situ Saturation Monitoring (ISSM).
- Relative Permeability by centrifugation (P&T)
- IOR/EOR (Low salinity, ASP,....)
- Trapped Gas Saturation with ISSM
- NMR measurements



## SCAL HPHT Reservoir Conditions with ISSM:

- USS and SS Relative Permeability with Live Fluids
- Water Alternating Gas Studies («WAG»)
- Gas Condensate Blockage Studies
- Critical Gas Saturation
- IOR/EOR (HC, CO<sub>2</sub>, N<sub>2</sub>, ASP, Low sal., ....)
- Miscible floods – Slim tube Experiments
- Miscible floods – Core Sample
- Interfacial tension (IFT)



{ Short introduction to Relative Permeability }





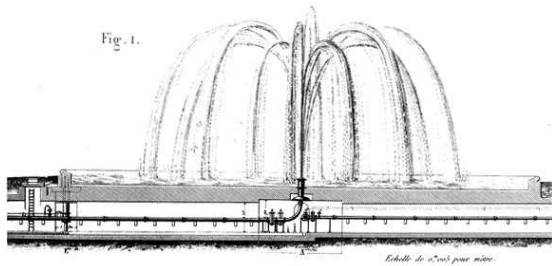
# Introduction to Relative Permeability

## Relative Permeability:

- Concept used to describe the movement of more than one fluid in a porous medium
- Basic description of how fluids move through the reservoir
- Understanding reservoir economics
  - Hydrocarbon recovery rate
  - Total recoverable reserves
  - Water cut

# Permeability Description

General expression for fluid flow developed by Henry Darcy in 1856



$$q = \frac{KA\Delta P}{\mu L}$$



Where:

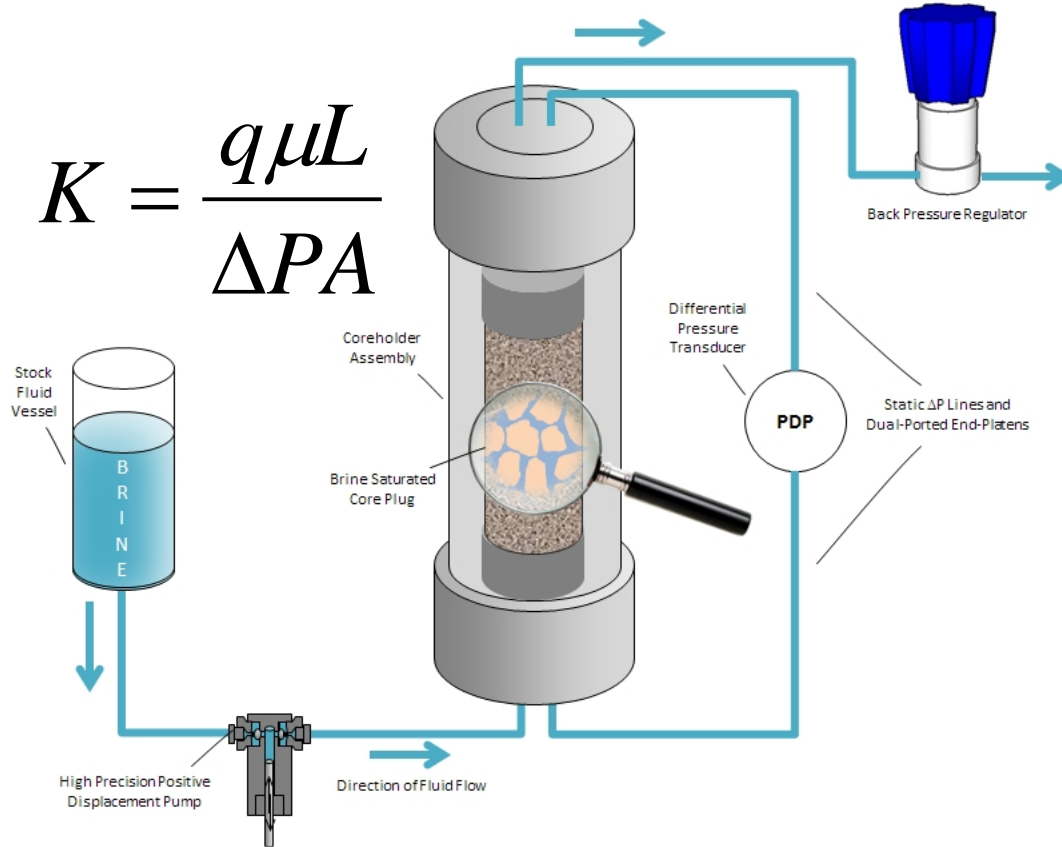
- $q$  = the rate of fluid flow ( $\text{m}^3/\text{s}$ )
- $A$  = cross-sectional area ( $\text{m}^2$ )
- $\mu$  = viscosity of the flowing fluid (cP)
- $\Delta P$  = pressure drop across the sample (Pa)
- $L$  = core length (m)
- $K$  = permeability ( $\text{m}^2$ )

$K$  is a constant when:

- the flow is laminar and Newtonian
- the fluid does not interact with the rock
- the rock is completely saturated and fluid continuous

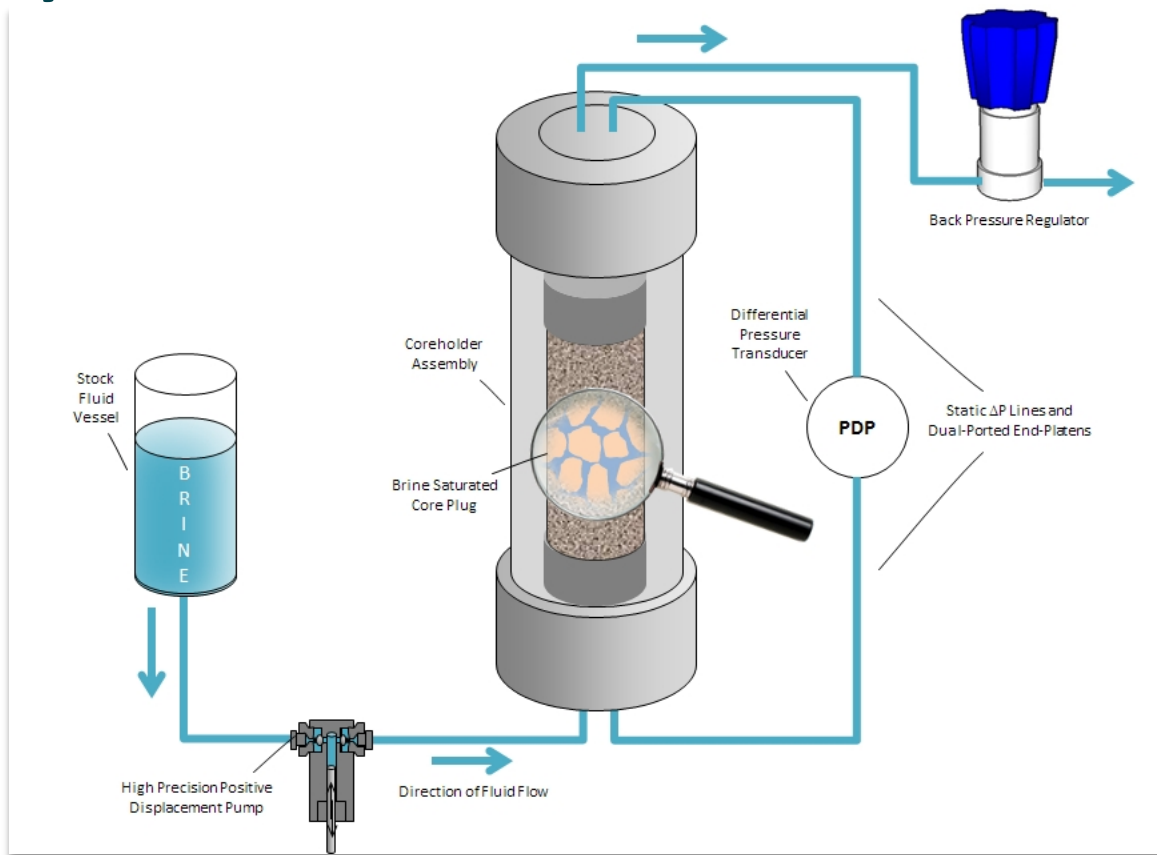
# Liquid permeability

$$K = \frac{q\mu L}{\Delta PA}$$



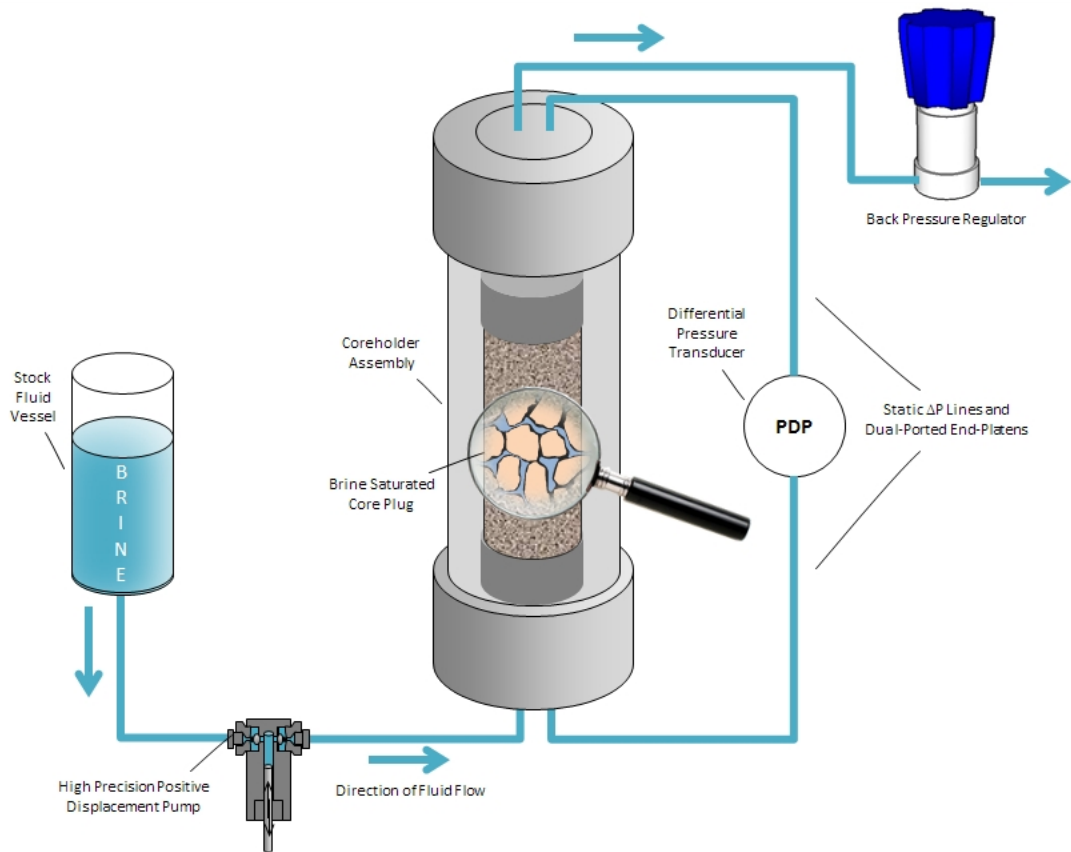
# Absolute permeability...

...is the permeability determined with only one fluid present in the pore space



# Effective permeability...

...is the permeability to one fluid, when there is more than one fluid present in the pore space

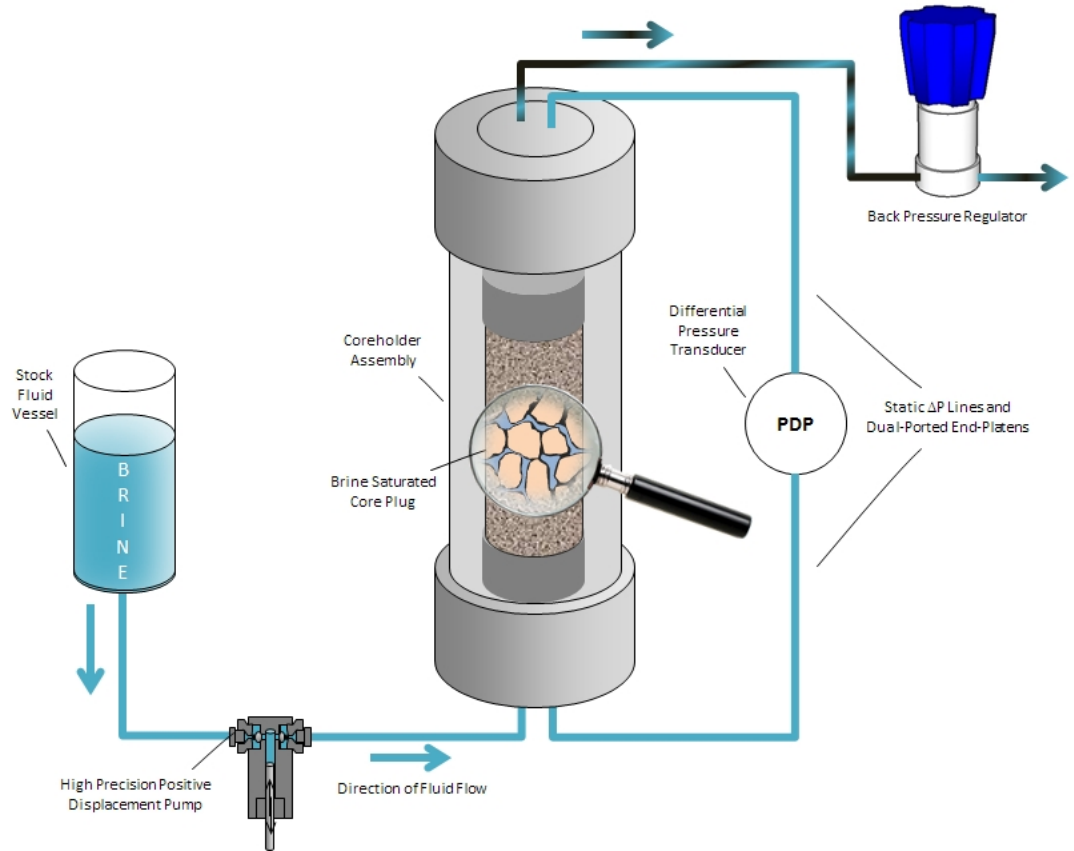


# Relative permeability...

...is the effective permeability divided by a specified base permeability

$$k_r = \frac{k_e}{k_{ref}}$$

...is a measure of the ability of the porous system to conduct a fluid when more than one fluid is present

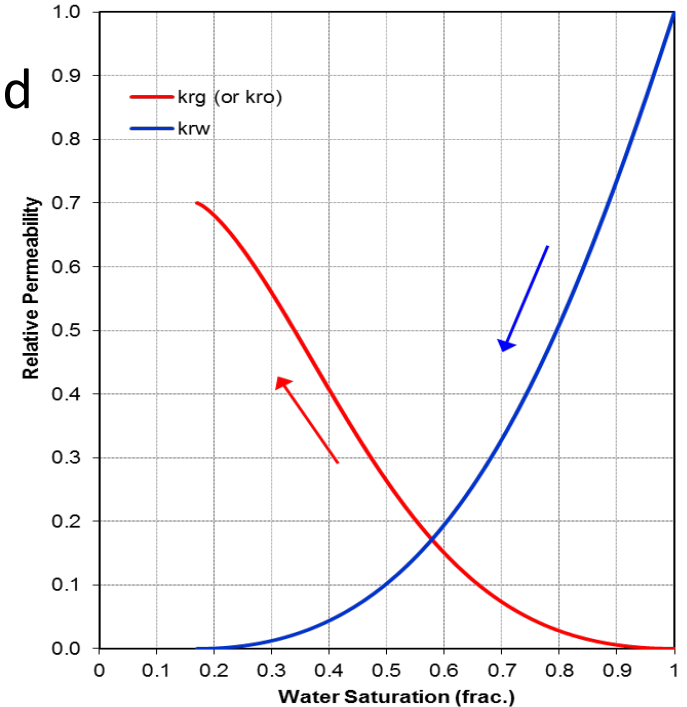
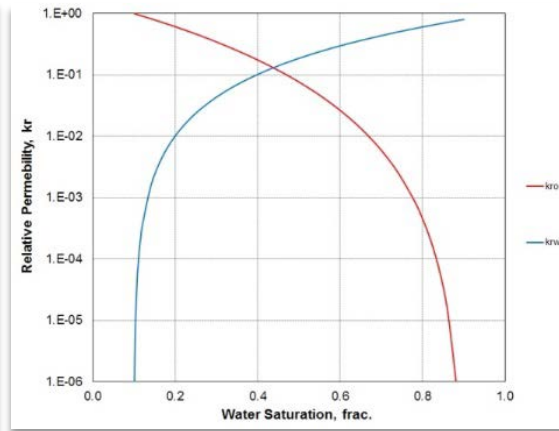
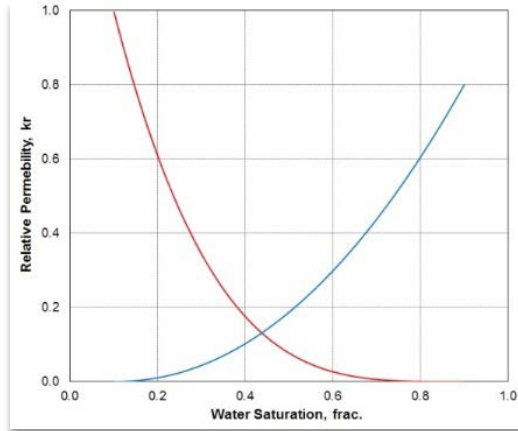




# Base (Reference) Permeability

Primary drainage :  $k_r$  usually normalised to  $K_w$

Imbibition (& secondary drainage)  $k_r$  is referenced to  $k_o(S_{wi})$

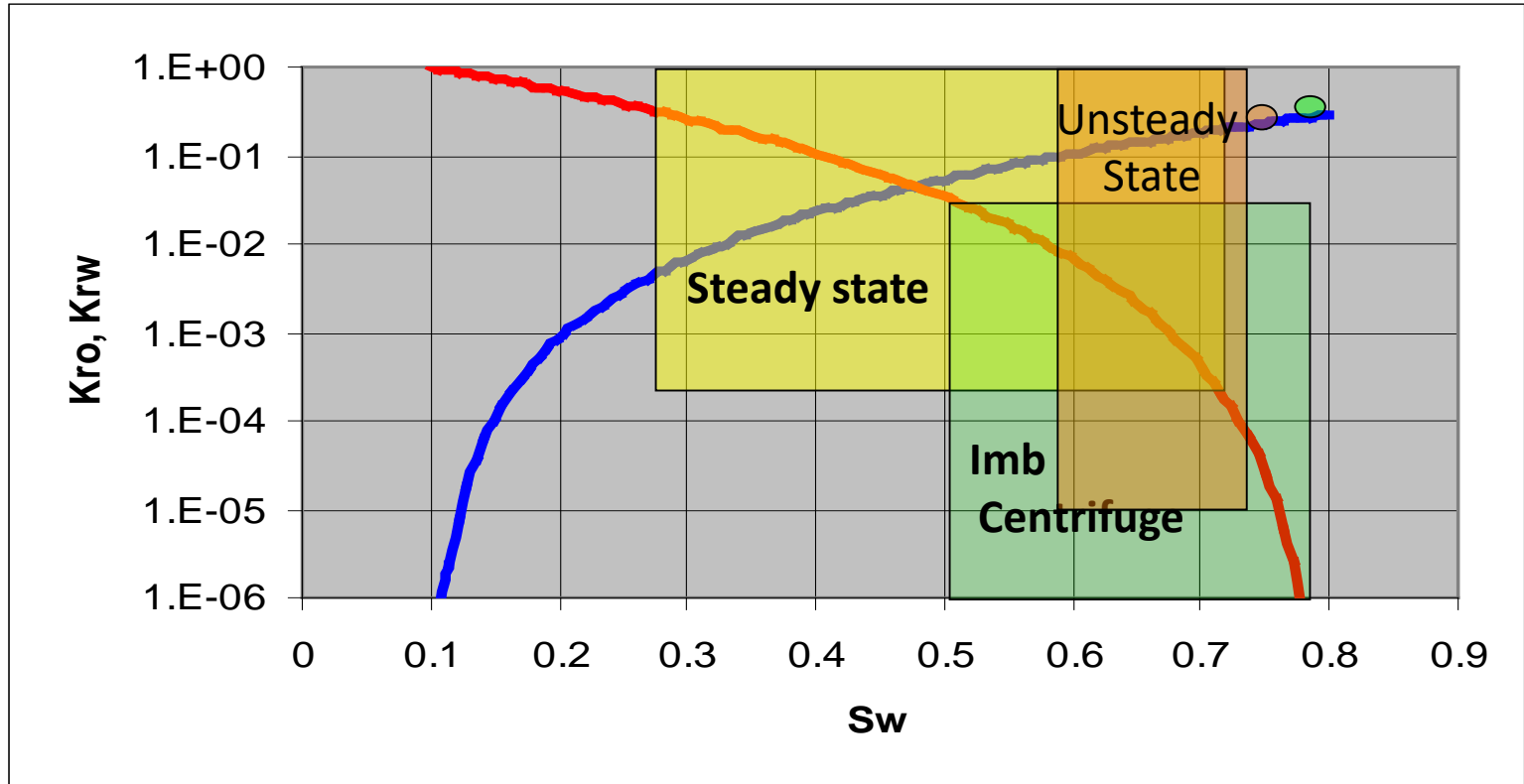


# Data for Reservoir Engineers - Dynamic Simulation

- Water-Oil Relative Permeability ( $k_{rw}$ - $k_{ro}$ )  
Water drive, water injection
- Gas-Oil Relative Permeability ( $k_{rg}$ - $k_{ro}$ )  
Solution gas drive  
Gas cap drive  
Gas injection
- Water - Gas Relative Permeability ( $k_{rw}$ - $k_{rg}$ )  
Aquifer influx into gas reservoir
- Gas-Water Relative Permeability ( $k_{rg}$ - $k_{rw}$ )  
Gas storage, CO<sub>2</sub> sequestration



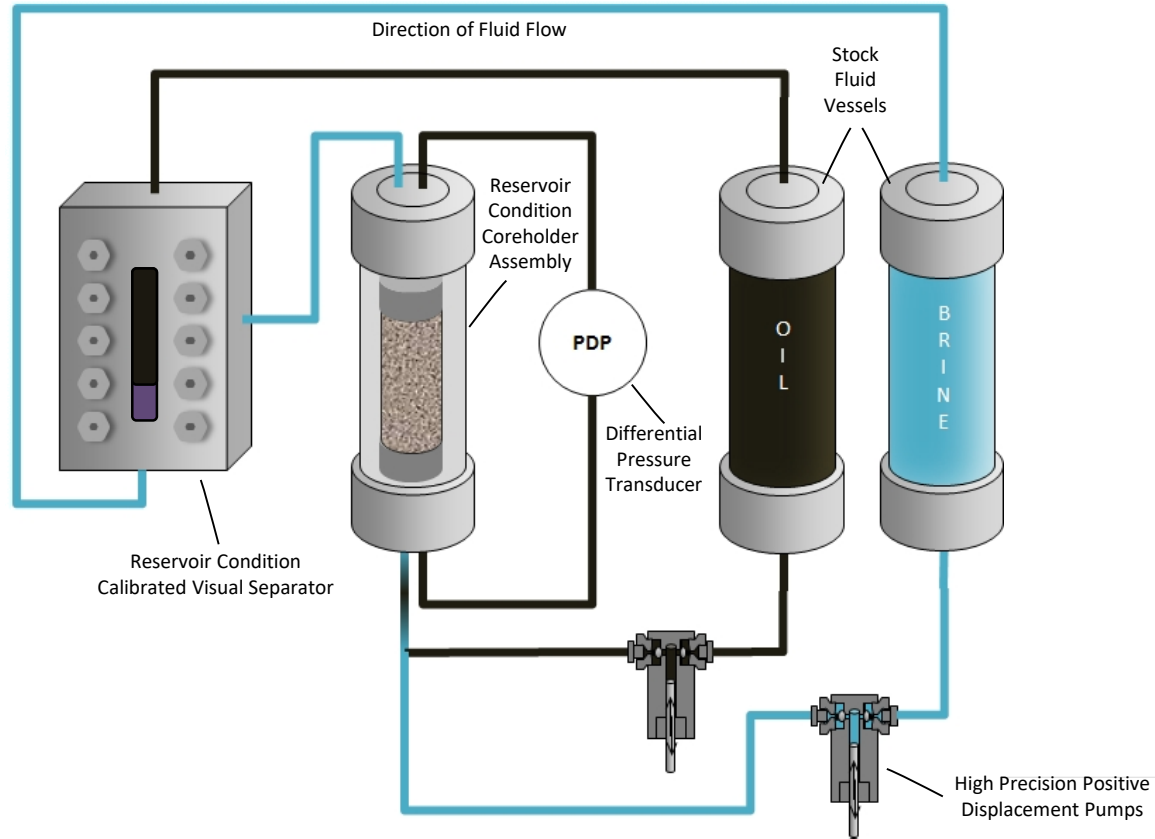
# Imbibition Relative Permeability



Relative Permeability by Steady State method

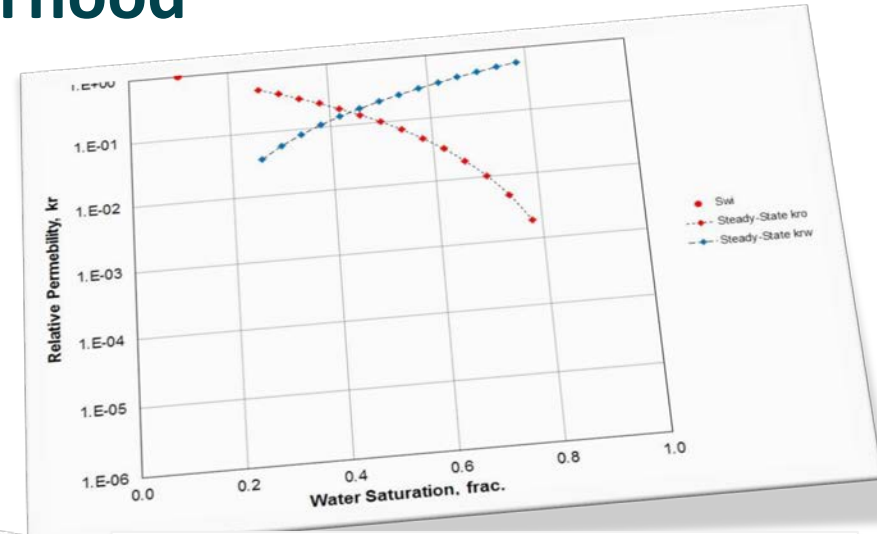
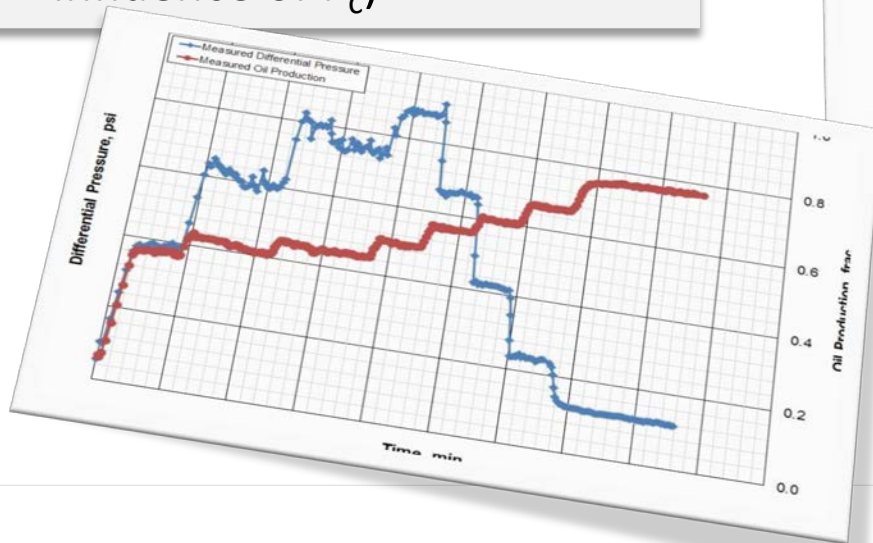


# Steady State Coreflood (SS)



# Steady State Imbibition Waterflood

- Continuous recirculation of injected brine & oil
- Higher flowrate possible with stable flow (minimise influence of  $P_c$ )



- Saturation from ISSM
- Calculate relative permeability directly from equilibrium  $\Delta P$  and individual phase flowrates



# Steady-state Overview

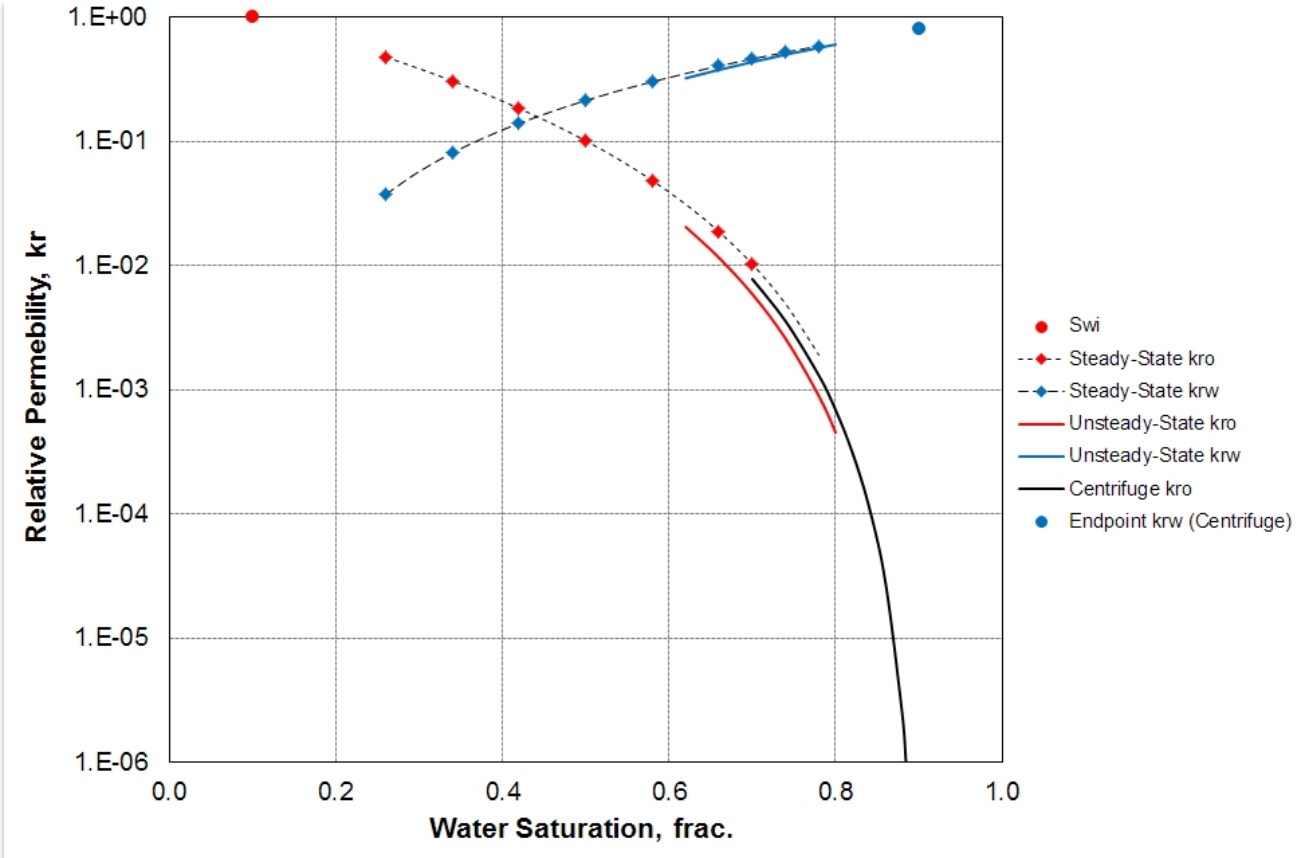
## Advantages

- Data interpretation and calculation is (usually) straight forward
- Extended saturation range possible to define relative permeability curve
- Higher flow rates may be used to mitigate laboratory scale capillary pressure
- Suitable for most wettability cases & reservoir oils

## Disadvantages

- Longer test required to achieve SS at each  $f_w$  (1 to 3 days per  $f_w$ )
- Uncertainty as to whether fluid displacement is truly representative of the reservoir process.
- Possible core damage due to large volume throughput (and high flow rate)
- Application of Darcy's Law is valid only if the saturation in the core is uniform (assumes  $P_c=0$ ).

# Centrifuge + USS + SS



# Typical outline

## Imbibition water displacing oil Relative Permeability

- Clean and dry core, measure basic properties
- Saturate core with brine, measure  $K_w$
- Desaturate to  $S_{wi}$
- Restore Wettability
- Measure endpoint (base) (multi-rate) permeability

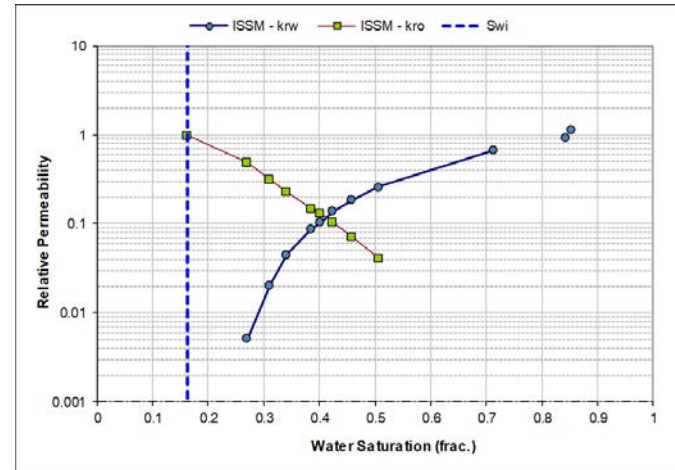
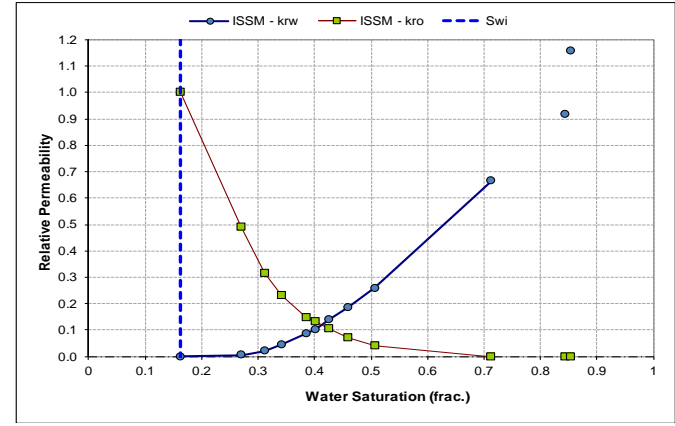
$$k_o(S_{wi})$$

- Measure Relative Permeability

$$k_w - k_o$$

- Measure endpoint (multi-rate) permeability

$$k_w(S_{or})$$



# Controlling Factors

## A number of factors influence Relative Permeability:

- Initial water saturation,  $S_{wi}$
- Wettability
- Pore structure – homogeneity of core material
- Saturation history (& hysteresis)
- Test procedures
- Laboratory length scale (capillary pressure)
- Mobility ratio

# Required Fluids

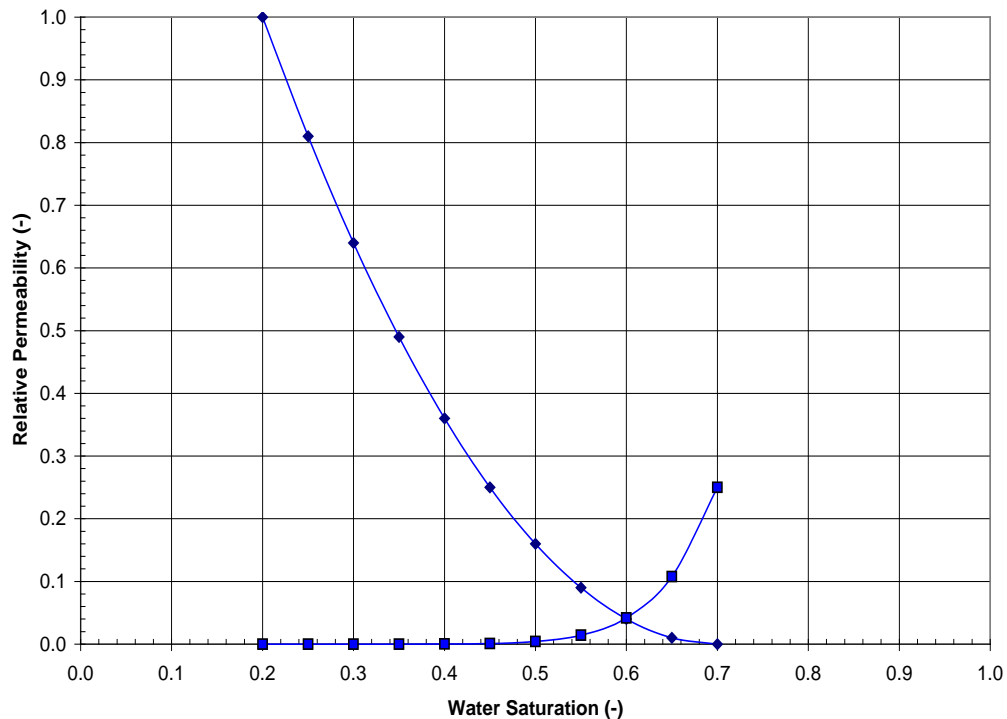
## Preparation of laboratory fluids Includes:

- a. Preparation of laboratory synthetic formation water (SFW) – Client to supply composition
- b. Preparation of CsCl doped synthetic formation water (dSFW)
- c. Preparation of CsCl doped injection water (if different from dSFW) – Client to supply composition
- d. Preparation of laboratory oil (Isopar-L) for ambient temperature measurements

## Preparation of live oil Includes:

- a. Preparation and measurement of Stock Tank Oil (STO) composition. – Client to supply surface oil
- b. Calculation & preparation of synthetic gas composition. – Client to supply PVT report
- c. Measurement QC of gas composition.
- d. Recombination of STO and synthetic gas to a specified B.Pt pressure.
- e. Recombined live oil composition, B.Pt, GOR, Bo (measurement QC).
- f. Viscosity measurement.

# Relative Permeability Curves - Effect of Wettability

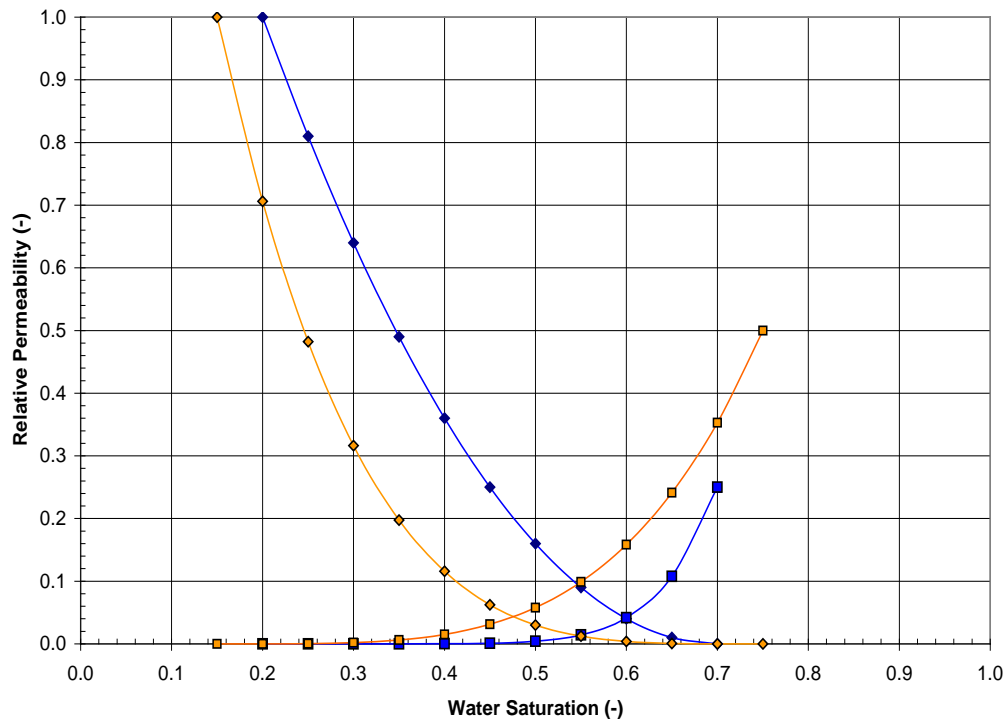


## Water Wet

- $N_o = 2$                        $N_w = 8$
- $S_{wir} = 0.20$                        $S_{ro} = 0.30$ ,
- $kr_w' = 0.25$ , ultimate recovery = 0.625 OIIP



# Relative Permeability Curves - Effect of Wettability



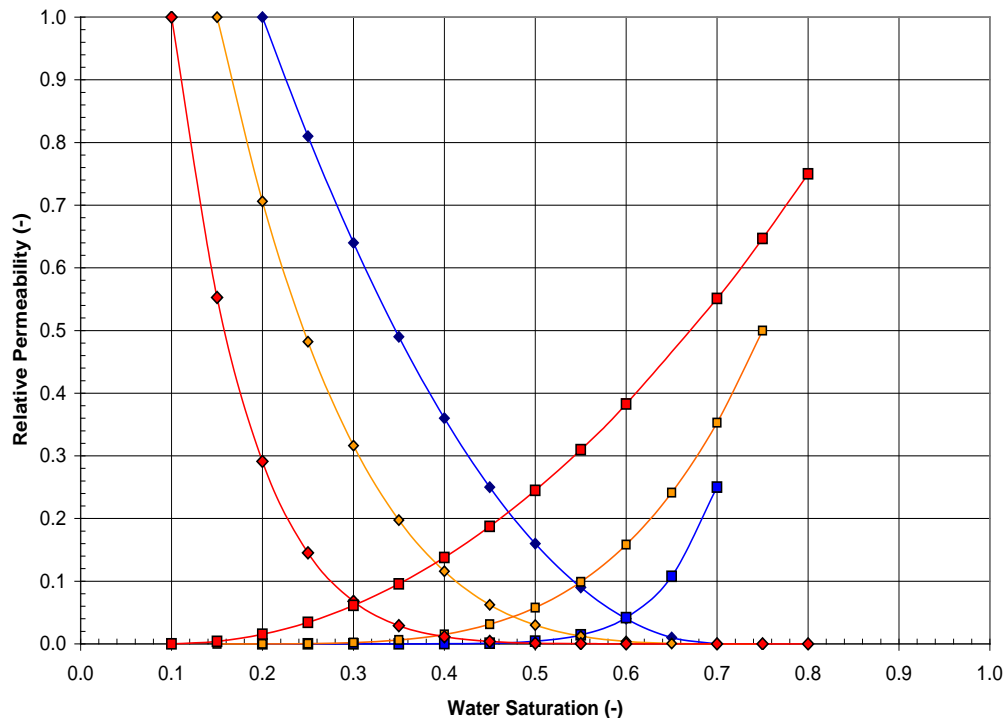
## Water Wet

- No = 2
- Swir = 0.20
- krw' = 0.25, ultimate recovery = 0.625 OIIP
- Nw = 8
- Sro = 0.30,

## Intermediate Wet

- No = 4
- Swir = 0.15
- krw' = 0.5, ultimate recovery = 0.706 OIIP
- Nw = 4
- Sro = 0.25,

# Relative Permeability Curves - Effect of Wettability



## Water Wet

- No = 2
- Swir = 0.20
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## Intermediate Wet

- No = 4
- Swir = 0.15
- krw' = 0.5, ultimate recovery = 0.706 OIIP
- Nw = 4
- Sro = 0.25,

## Oil Wet

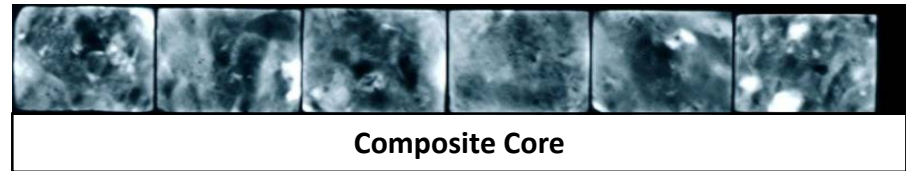
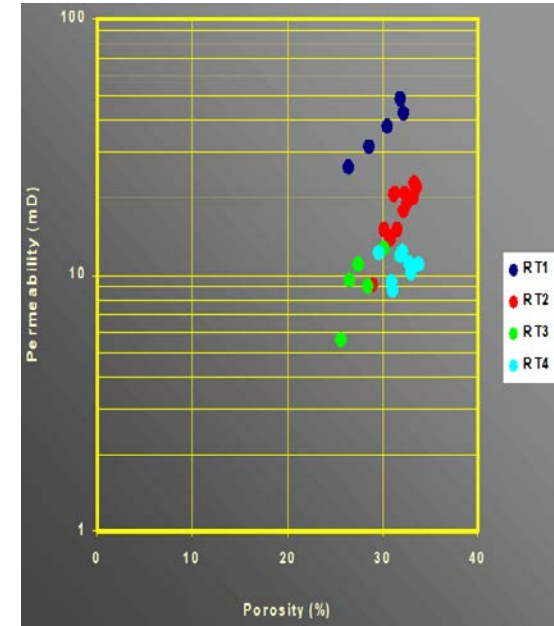
- No = 8
- Swir = 0.10
- krw' = 0.75, ultimate recovery = 0.778 OIIP
- Nw = 2
- Sro = 0.20,

# Selection of core material

## Select representative homogeneous core material

Samples screening and evaluation is needed to perform a proper selection of suitable and representative samples.

- Homogeneity screening (representativity)
- Characterize rock samples and identify representative lithology/rock type
  - 1 rock type per test
- Location of samples reference to reservoir
- All available information and data should be evaluated to be able to perform a proper samples selection, such as
  - CT scan,
  - Basic properties
  - lithological description, formation/zone, hydrocarbon leg (Gas, Water, Oil)
  - MICP, XRD, etc.



# Preparation of core material

## Cleaning and drying

### Preparation Methods

- Restored State Preparation
- Native State Preparation
- Cleaned State Preparation

### Considerations for Preparation

- How was the core drilled? (mud type, coring operations, well-site work)
- How the core was handled and preserved

### Restored state preparation

- Cleaning and drying methods adapted to clay content and mineralogy
- If sensitive clay materials – consider non-drying route
- Saturate with appropriate brine
- Establish representative initial water saturation
- Restore wettability with live reservoir oil



# Centrifuge Drainage to Swi

## Methods

### 1. Drainage by Centrifuge

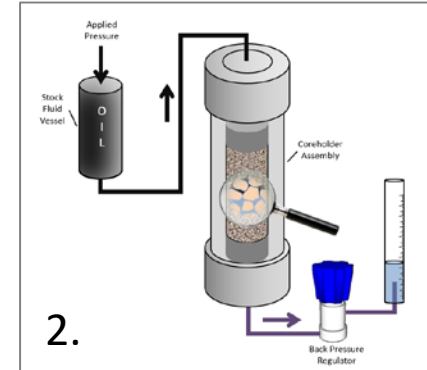
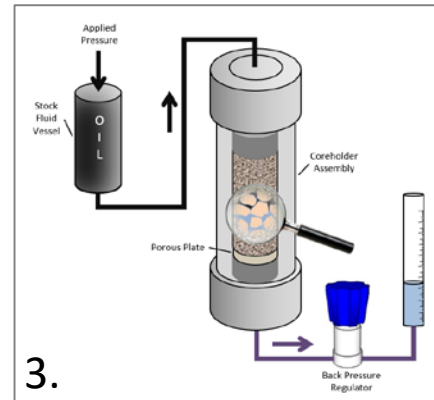
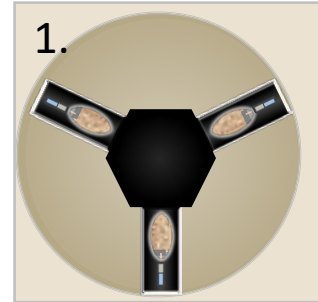
- i. Fast, suitable for low permeable core material
- ii. End effect on saturation distribution

### 2. Drainage by Viscous oil drive

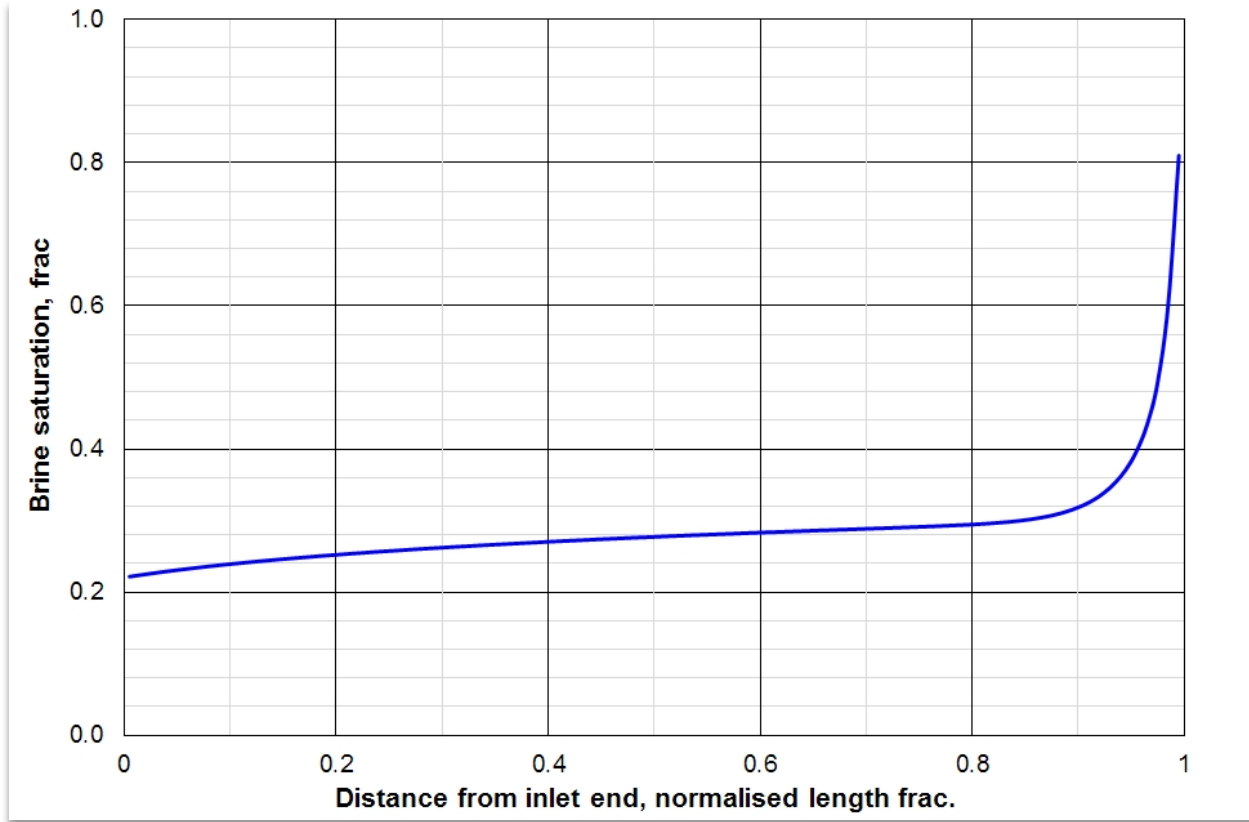
- i. Fast, suitable for unconsolidated core material
- ii. End effect on saturation distribution
- iii. Can give too high Swi

### 3. Drainage by porous plate – preferred method

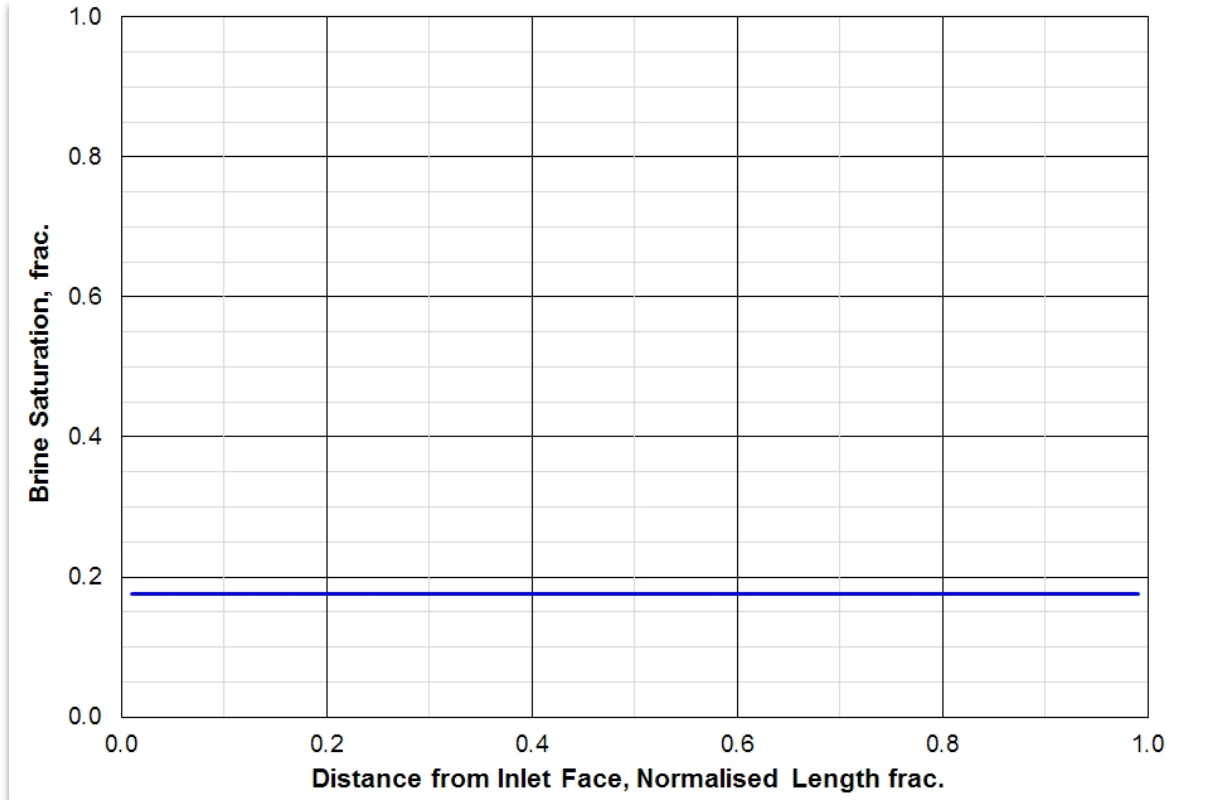
- i. Gives homogeneous water saturation
- ii. Pc, limited by porous plate, but suitable for most cases
- iii. Takes longer time – but full PcRI not required when using to prepare for relative permeability measurements



# Without Porous Plate



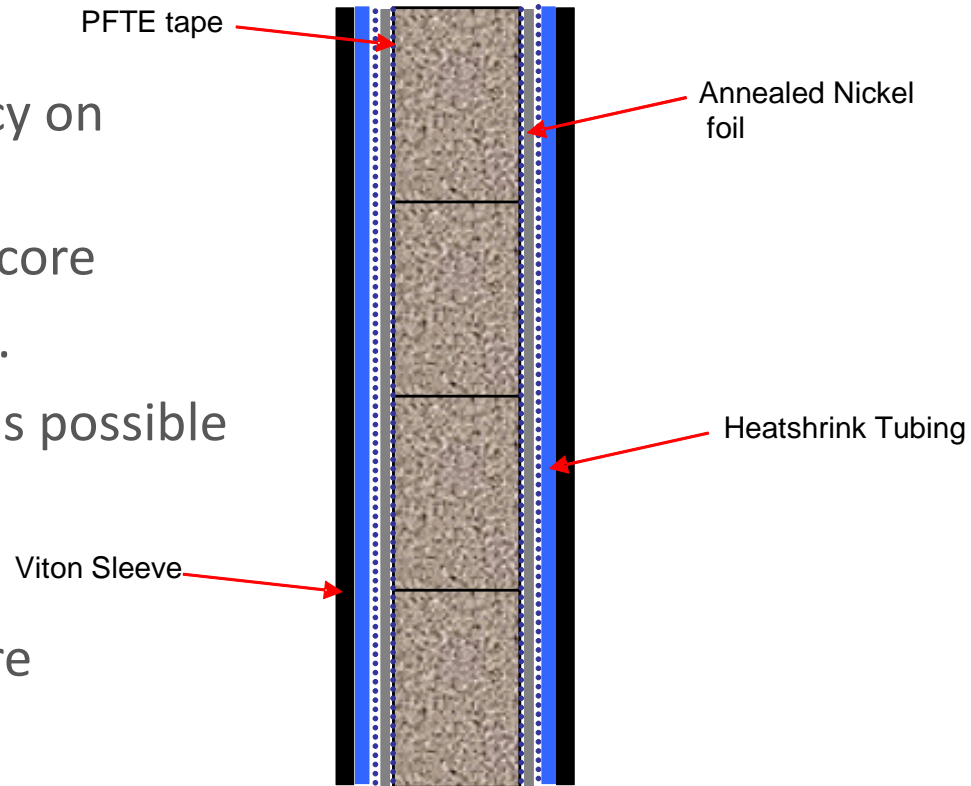
# With Porous Plate



# Composite core

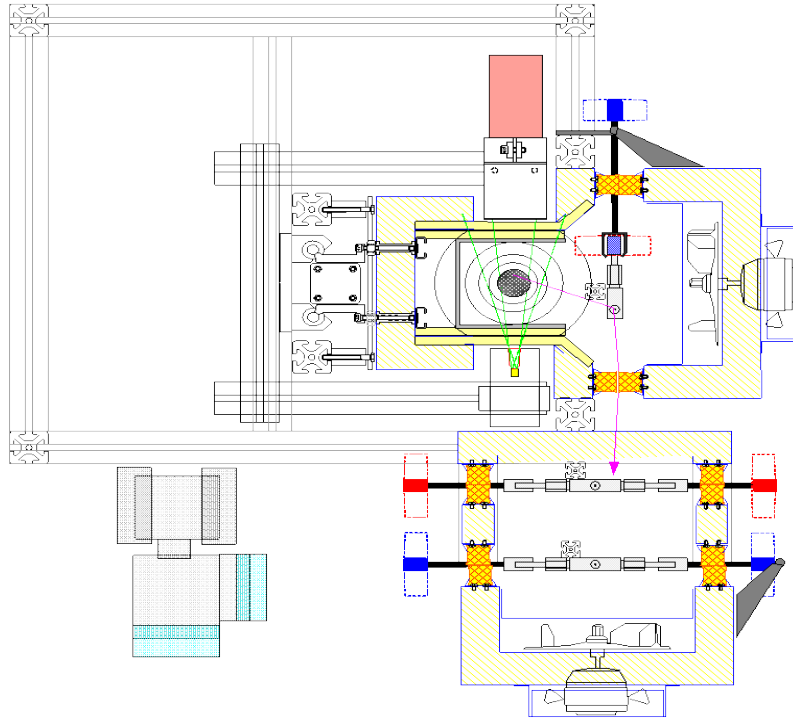
## Composite core advantages and disadvantages

- For flood type tests
- Larger pore volume, higher accuracy on volumetric measurements
- Higher differential pressure across core
- Less impact of capillary end effects.
- Plug samples should be as similar as possible
  - Porosity, permeability
  - Saturation,
  - Pore size distribution
- Risk of effect of discontinuity in core junctions





# Reservoir Condition Core Flood Rig



# Core Flooding

## Saturation Determined by:

### External Methods

- Volumetric (Visual Cell/Separator)

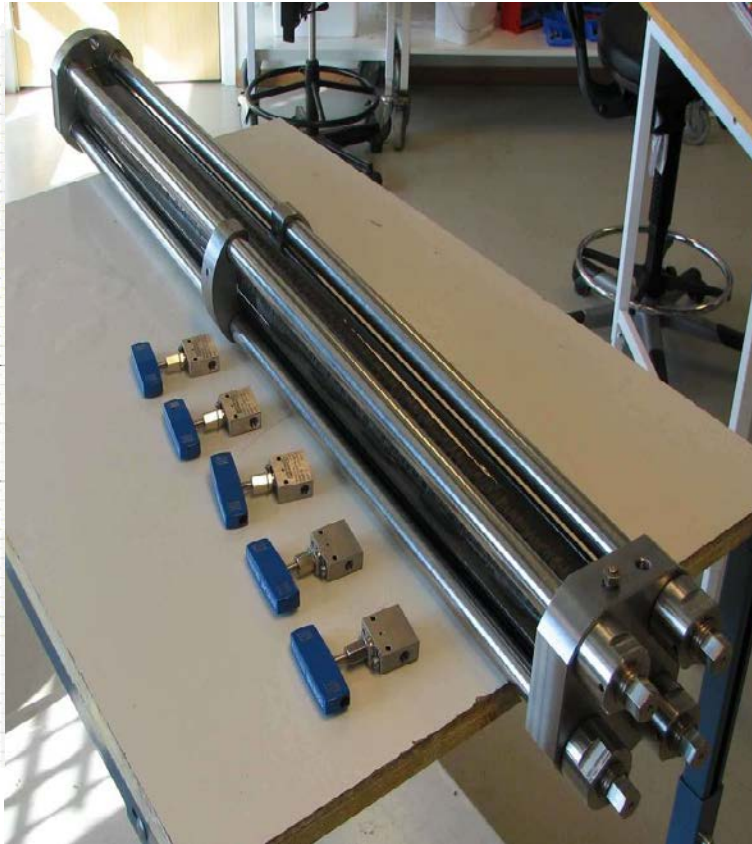
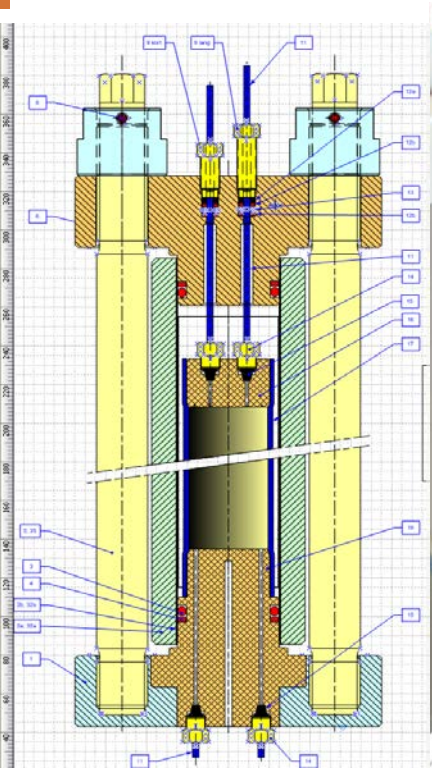
- Solvent extraction and Karl Fischer titration – end point

### In-situ Methods

- Gamma ray attenuation

- Tracer Techniques – end point

# Stratum Reservoir Carbon Fibre Core Holders

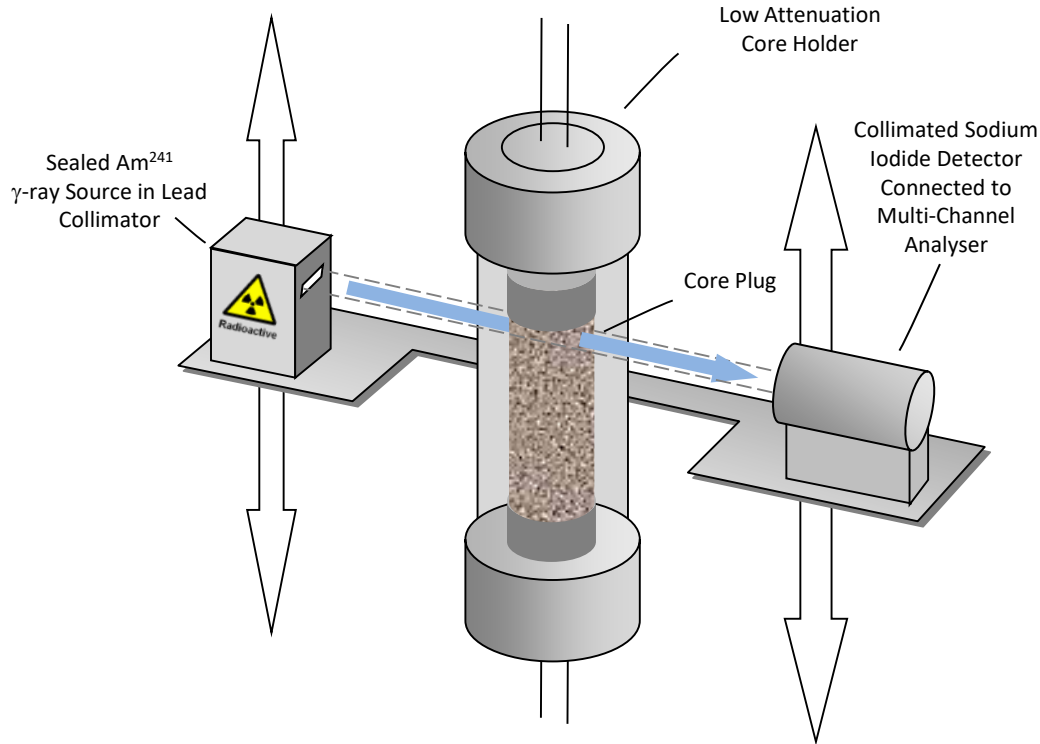


1000bar 170°C Model



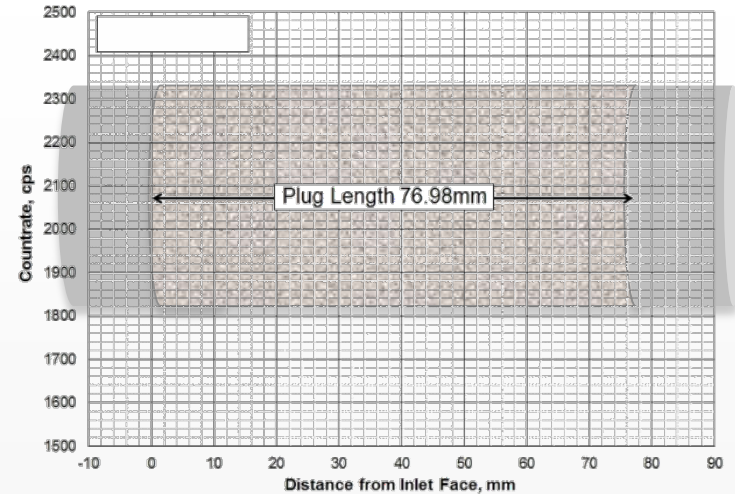
700bar 150°C Model

# In-Situ Saturation Monitoring (ISSM)

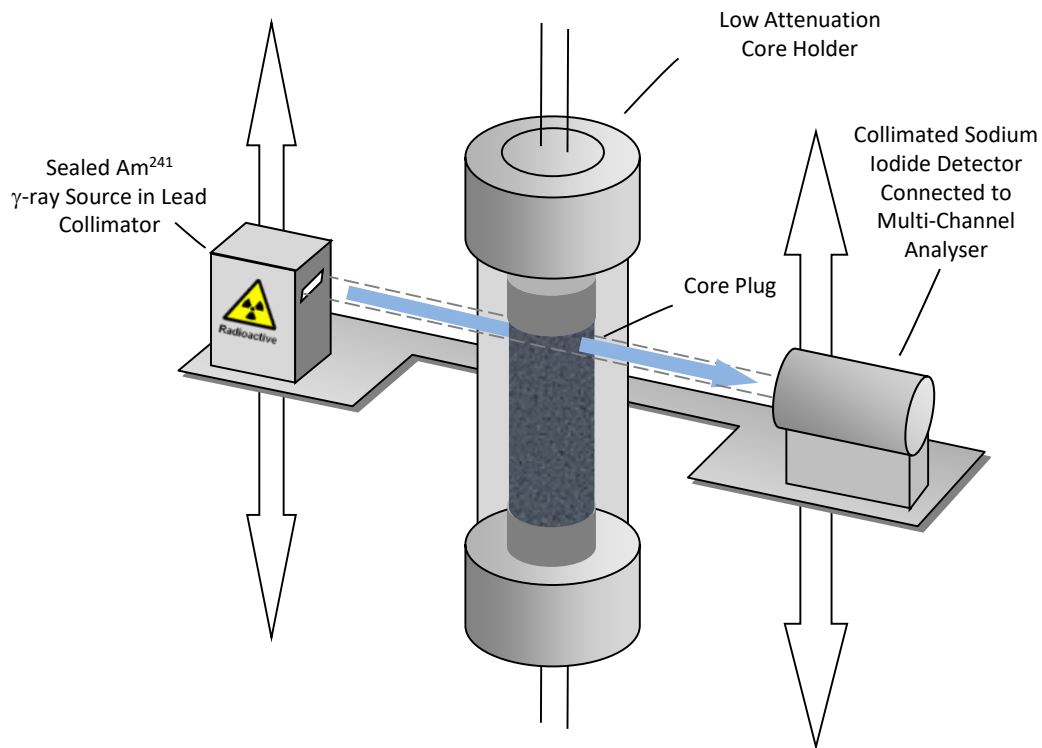


$$I_{\text{(transmitted)}} = I_i \cdot e^{-\mu x}$$

$$I_{\text{(transmitted)}} = I_i \cdot e^{-\{\mu x(1-\phi) + \phi x(S_{w,\mu w} + S_{o,\mu o})\}}$$

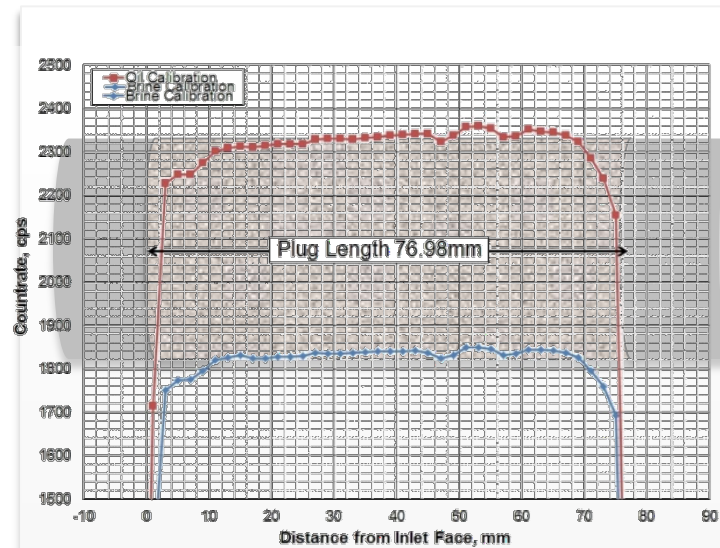


# In-Situ Saturation Monitoring (ISSM)



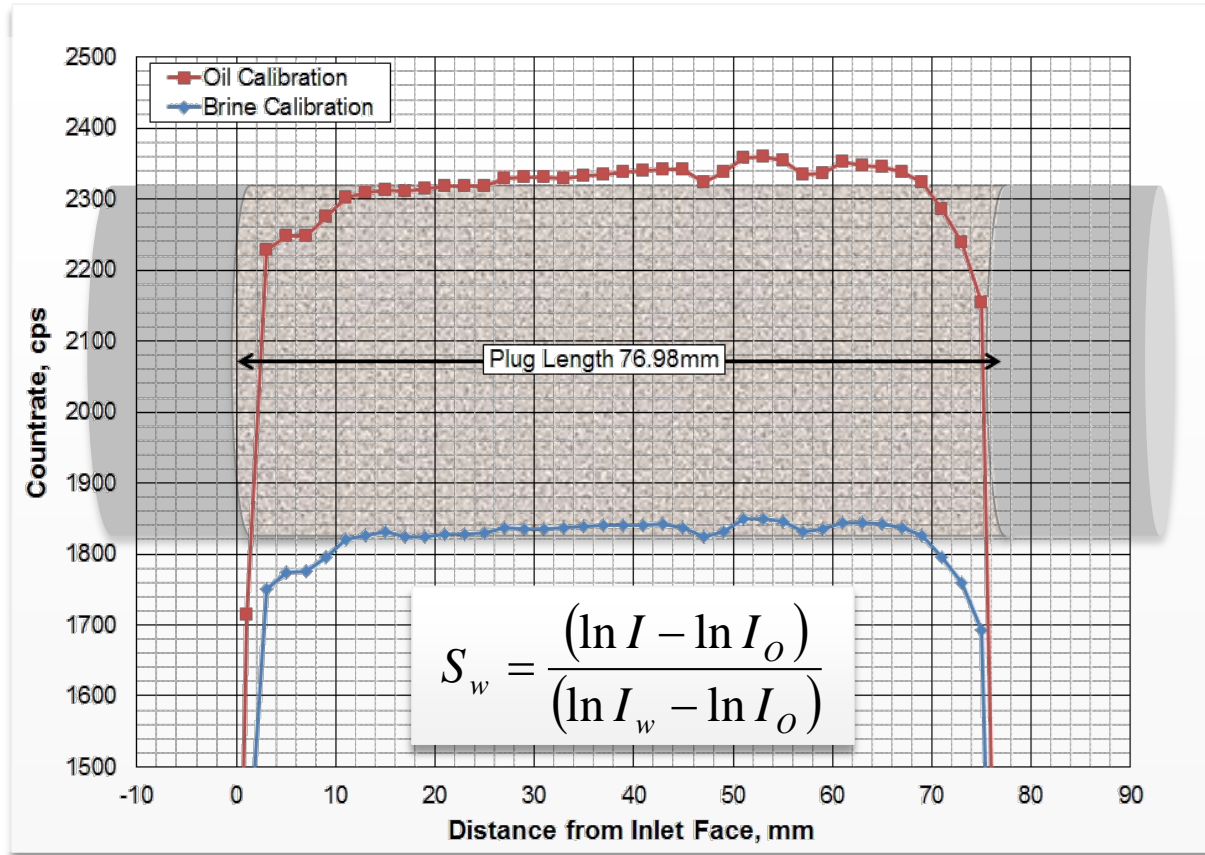
$$I_{(transmitted)} = I_i \cdot e^{-\mu x}$$

$$I_{(transmitted)} = I_i \cdot e^{-\{\mu x(1-\phi) + \phi x(S_{w,\mu w} + S_{o,\mu o})\}}$$

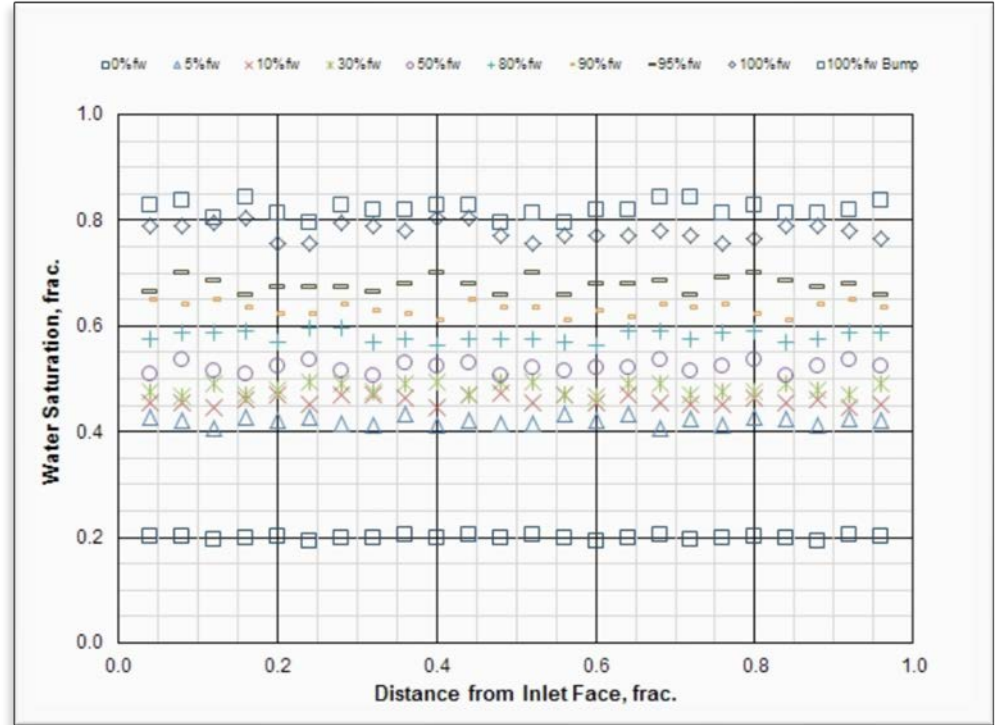
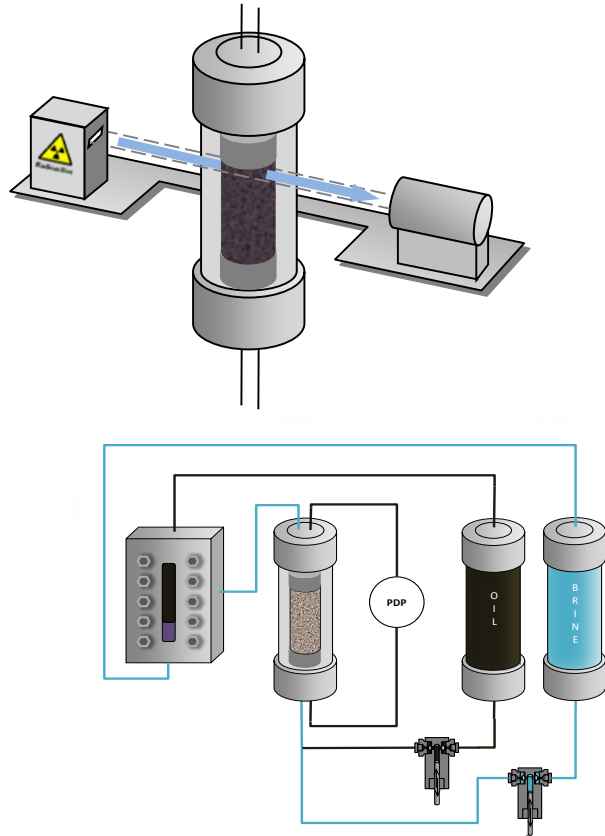




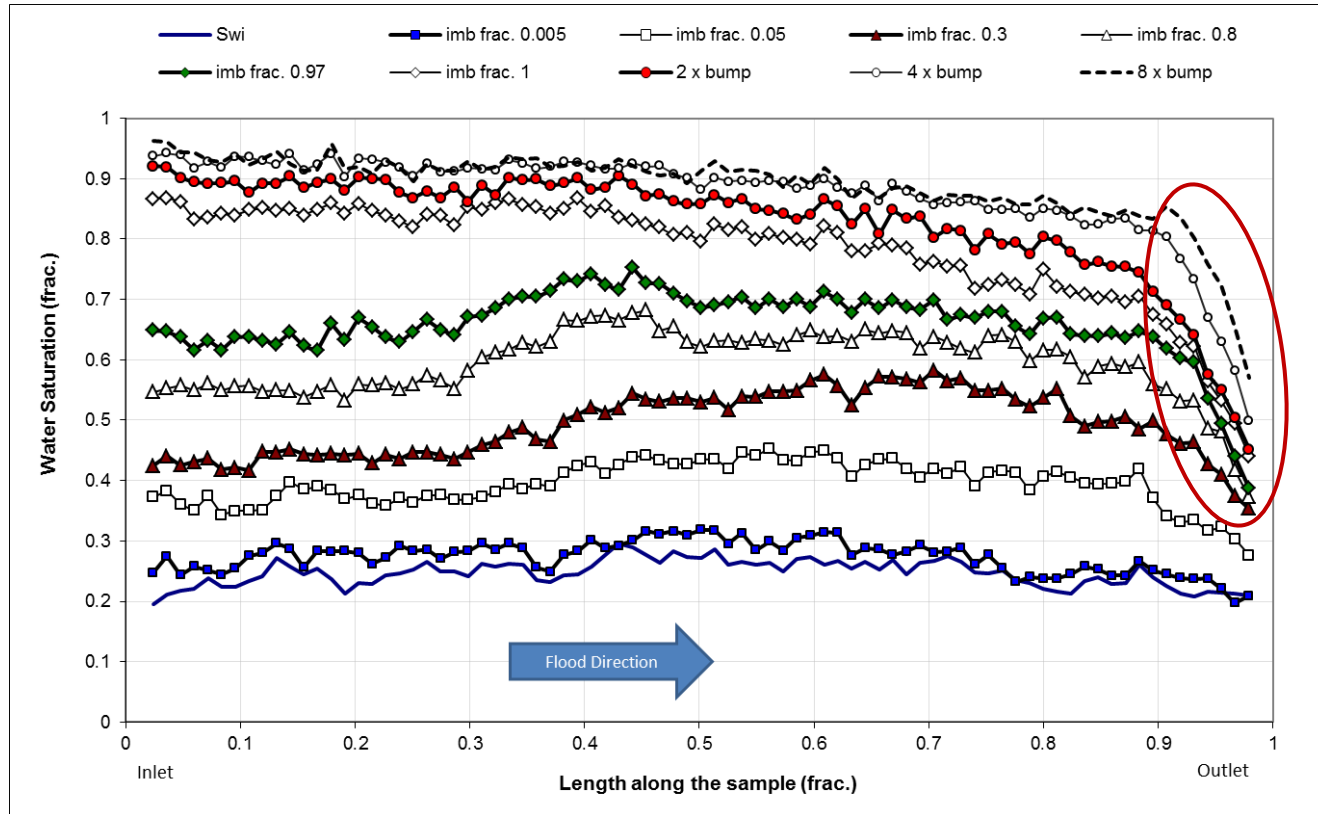
# In-Situ Saturation Monitoring (ISSM)



# ISSM For Steady-state Core Flooding



# Laboratory Effects





# Relative Permeability Models

## Corey Relative Permeability Model:

$$k_{ron} = \frac{k_{ro}}{k_{ro}'} = S_{on}^{N_o}$$

$k_{ro}'$  = end-point  $k_{ro}$

$$k_{rwn} = \frac{k_{rw}}{k_{rw}'} = S_{wn}^{N_w}$$

$k_{rw}'$  = end-point  $k_{rw}$

$$S_{wn} = \frac{S_w - S_{wir}}{1 - S_{wir} - S_{ro}}$$

$$S_{on} = \frac{1 - S_w - S_{ro}}{1 - S_{wir} - S_{ro}} = 1 - S_{wn}$$

Typical properties for different wettability conditions

Condition	$S_{wi}$ (%)	$S_{or}$ (%)	$k_{rw}'$	$n_w$	$n_o$
Water wet (WW)	> 20 -25	< 10	0.1 - 0.4	4 - 6	2 - 3
Mixed wet (MW)	15-25	10-15	0.5 - 0.9	2 - 4	3 - 5
Oil Wet (OW)	< 15	> 15	0.8 - 1.0	1.5 - 3	6 - 8

# Relative Permeability Models

## LET Relative Permeability Model:

$$k_{rw} = k_{rw}^0 \frac{(S_w^*)^{L_w}}{(S_w^*)^{L_w} + E_w(1 - S_w^*)^{T_w}}$$

$$k_{ro} = k_{ro}^0 \frac{(1 - S_w^*)^{L_o}}{(1 - S_w^*)^{L_o} + E_o(S_w^*)^{T_o}}$$

$$S_w^* = \frac{S_w - S_{wi}}{1 - S_{or} - S_{wi}}$$

### Constraints:

- $L_w \geq 1.0$  ,  $E_w \geq 0.5$ ,  $T_w \geq 0.5$
- $L_o \geq 1.0$  ,  $E_o \geq 0.5$ ,  $T_o \geq 0.5$

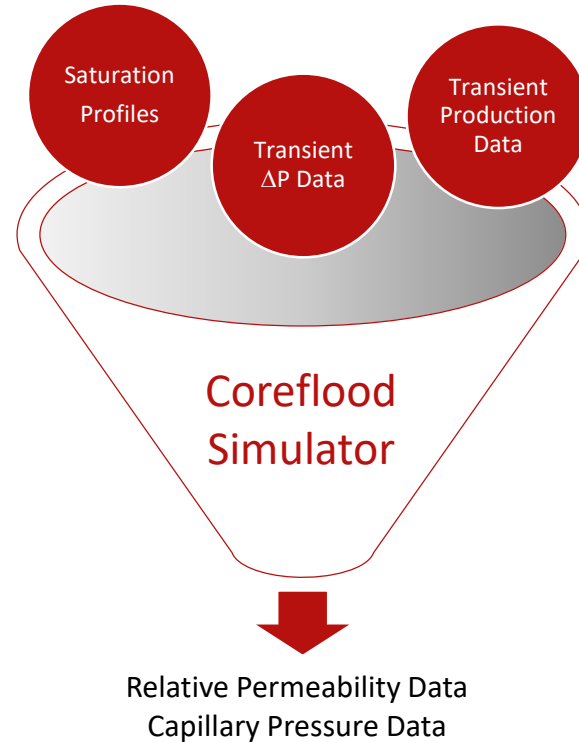
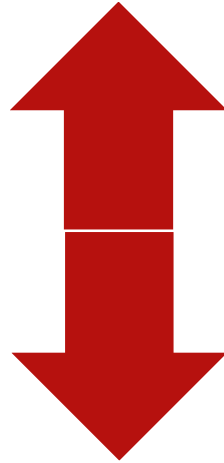
where:

- $k_{rw}$  - water relative permeability
- $k_{ro}$  - oil relative permeability
- $k_{rw}^0$  - water relative permeability at residual oil saturation
- $k_{ro}^0$  - oil relative permeability at initial water saturation
- $S_w$  - water saturation
- $S_w^*$  - normalised water saturation
- $S_{wi}$  - initial water saturation
- $S_{or}$  - residual oil saturation
- $L_w, E_w, T_w$  - LET parameters for water
- $L_o, E_o, T_o$  - LET parameters for oil

# History Matching Laboratory Data by Simulation

Quality Control of  
Laboratory Data

Useful Reservoir  
Engineering Data



# Core Flood Simulator

File View Project Tools Help

Properties (Inlet) 1.1 Corey / Skjæveland

Total Time 1000.000 min

Time	Water rate	Oil rate	Ramp time
min	ml/min	ml/min	min
0	0.1	0.9	0.000000
120	0.2	0.799998	0.000000
180	0.5	0.5	0.000000
240	0.799998	0.2	0.000000
300	0.9	0.1	0.000000
360	0.949998	0.05	0.000000
420	1	0	0.000000

Project Explorer

Special Core Analysis Project Elements

- Project LPS Seminar
  - Experiments
    - ANO 1
      - Setup
        - Porosity
        - Base permeability
        - Initial saturation
        - Grid
        - Inlet
        - Fluids
      - Experimental data
    - Analyses
      - 1 Sendra Analysis
        - Reference data
          - Ref: ANO 1
        - Flow properties
          - 1.1 Corey / Skjæveland
            - (1.1) ANO 1 Sim Differential pressure
            - (1.1) ANO 1 Sim Oil production
            - (1.1) ANO 1 Sim Water saturation
      - Plots
        - 1. Plot

Relative permeability: Corey

Capillary pressure: Skjæveland

Parameters for relative permeability

	Value	Min	Max
$N_w$	4	1	15
$N_o$	4	1	15
$k_{rj}(S_{wj})$	0.5	0	1
$k_{rj}(S_{oj})$	1	0	1

Saturation values

	Value	Min	Max
$S_{wi}$	0.15	0	1
$S_{wr}$	0.25	0	1

Parameters for capillary pressure

psi	Value	Min	Max
$C_w$	1	0	inf
$A_w$	0.25	0.25	2
$C_o$	1	0	inf
$A_o$	0.33	0.25	2

Use individual Swi

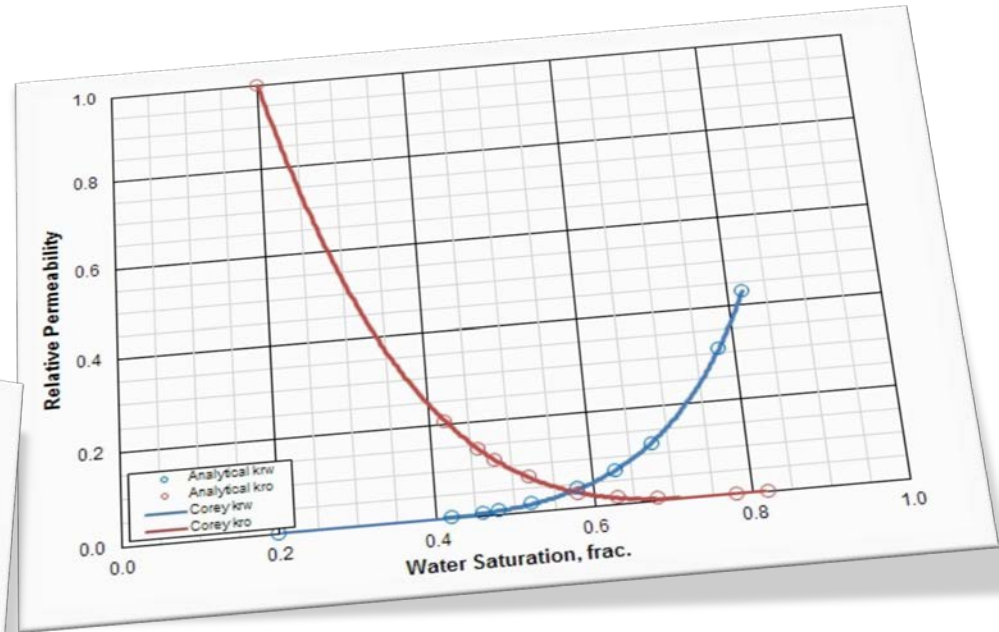
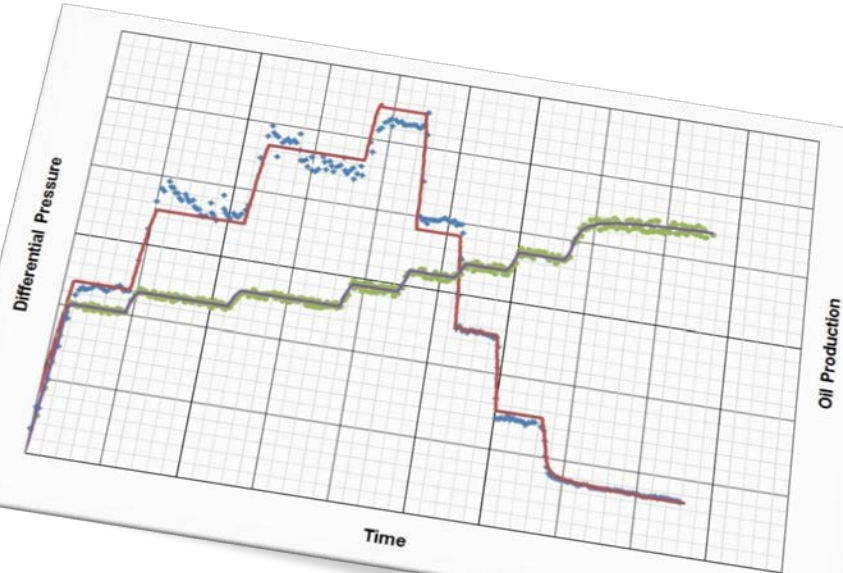
Use individual Sor

	Value	Min	Max
$S_{wi}$	0.2	0	1
$S_{wr}$	0.1	0	1

(1.1) ANO 1 Sim Oil production

# Simulation of Transient Data

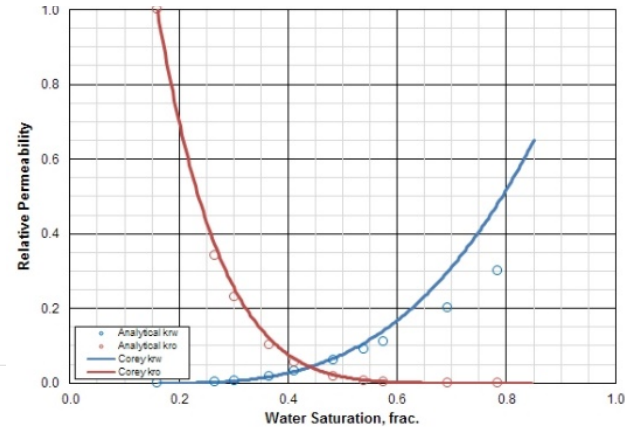
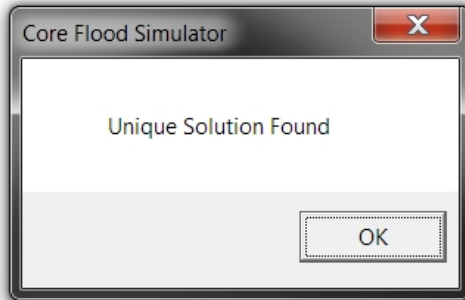
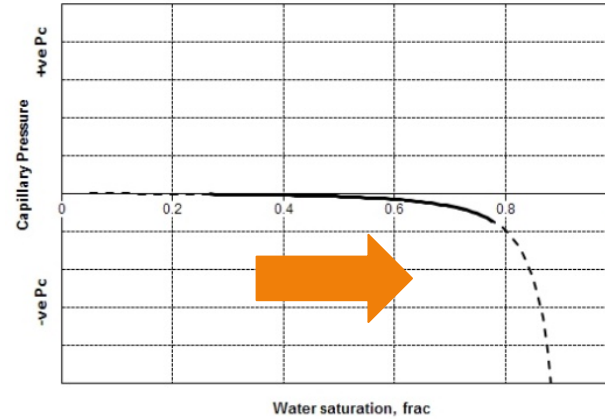
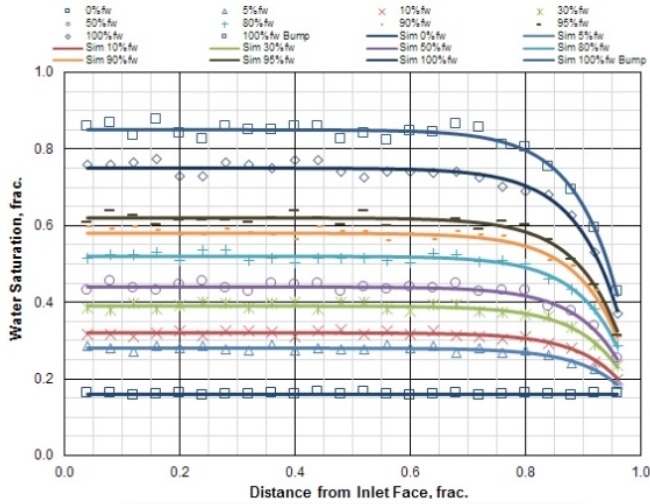
History matching of oil production and  $\Delta P$  transient data to derive  $k_{rw}$  &  $k_{ro}$



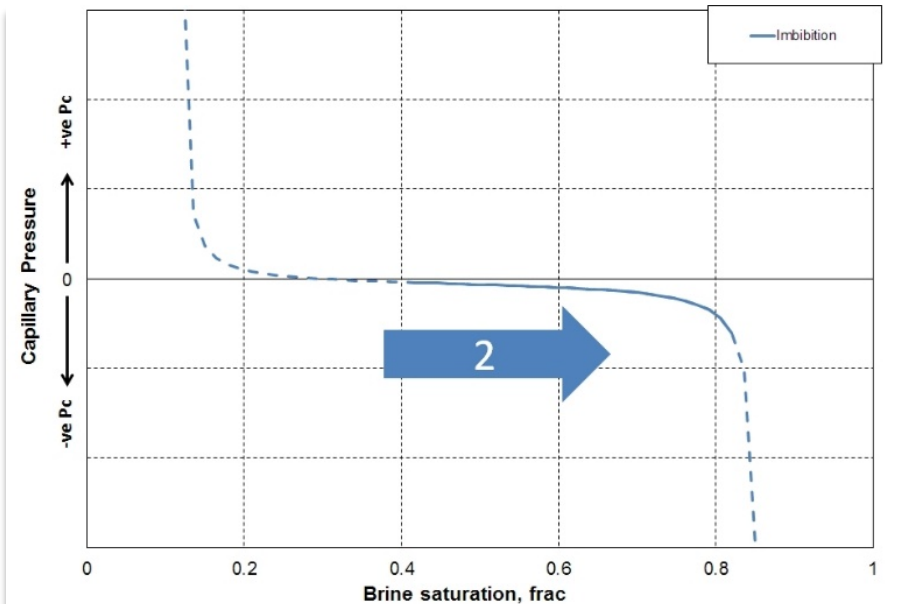
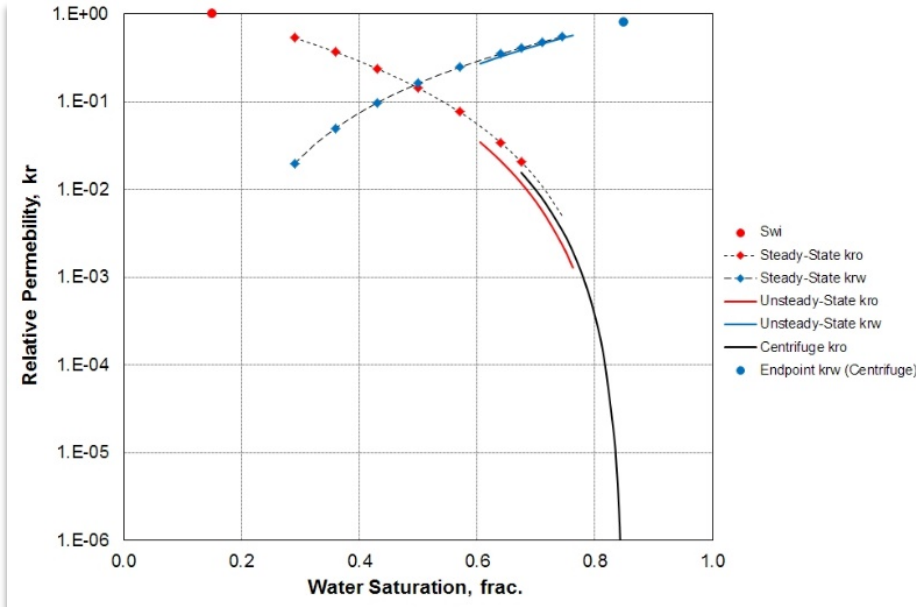
Estimation



# Case History 2 (Negative Imbibition Pc; Oil Wet)



# Data for the Reservoir Engineer



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**Thank you!**



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**Questions?**

[Helene.Auflem@stratumreservoir.com](mailto:Helene.Auflem@stratumreservoir.com)